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# Alternative Inverse Perspective Mapping Homography Matrix Computation for ADAS Systems Using Camera Intrinsic and Extrinsic Calibration Parameters

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## Abstract

This paper presents a simple novel IPM matrix computation method, which does not require any additional solutions to calculate homography matrices. This method only requires determining the distance from camera to projecting surface. It's simplicity allows execution even on very small energy-efficient embedded device processors without use of complex libraries such as OpenCV, that cannot be deployed there. Furthermore, it has strictly analytical solution, which allows avoidance of false optimums that are probable in heuristic methods for optimization. We provide formulas, that are easy transferable to any device and can be calculated using standard math libraries.

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**Keywords:** IPM; Homography; Bird eye view; calibration; projection

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## 1. Introduction

Advanced Driver Assistance Systems (ADAS) are getting more popular each year. They are a necessity for most modern vehicles. With help of these systems, dangerous road accidents can be greatly reduced. Currently there are two tasks in driver assistance system that require a "birds-eye-view" from the camera. These tasks are surround view ([1], [2]) and lane departure warning [3]. With their help driver can more fully assess environment around the vehicle and receive notifications in case of breaking the law.

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### 2. Existing solutions

Most common method for "birds-eye-view" image construction are perspective transformation matrices. When working with a two-dimensional space four reference points are selected and after that, their position on a transformed image is specified. Based on this information system of linear equations is built. Its solution provides the necessary coefficients to build a transformation matrix. These systems can be solved with the help of neural networks [4], as well as least squares method [5]. Paul Heckbert proposed analytical solution for this system by solving it's particular case in general and then acquiring general solution by combining particular cases [6]. This method has one caveat: when building a "birds-eye-view" three-dimensional space is required, whereas  $3 \times 3$  matrix provides only 2-dimensional transformations. This is why LDWS mainly use  $3 \times 4$  matrices [5]. The main idea is coordinate transformation and their further projection on an image surface ([7] and [8]). Main cons of this approach is relatively more demanding computations and lack of hardware solutions ([9] and [10]).

### 3. Proposed method

The main idea is to combine these two approaches. For efficiency  $3 \times 3$  matrices will be used, and for construction parameters for  $4 \times 3$  matrices will be used. Perspective transformations using matrices are described in (1) and (2).

$$\begin{pmatrix} x' \\ y' \\ z' \end{pmatrix} = \begin{pmatrix} a & b & c \\ d & e & f \\ g & h & 1 \end{pmatrix} * \begin{pmatrix} X \\ Y \\ 1 \end{pmatrix}, x = \frac{x'}{z'}, y = \frac{y'}{z'} \tag{1}$$

$$\begin{pmatrix} X' \\ Y' \\ Z' \end{pmatrix} = R * \begin{pmatrix} X \\ Y \\ Z \\ 1 \end{pmatrix}, R = \begin{pmatrix} r_{11} & r_{12} & r_{13} & t_x \\ r_{21} & r_{22} & r_{23} & t_y \\ r_{31} & r_{32} & r_{33} & t_z \end{pmatrix}$$

$$\begin{pmatrix} x' \\ y' \\ z' \end{pmatrix} = \begin{pmatrix} f_x & 0 & c_x \\ 0 & f_y & c_y \\ 0 & 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} X' \\ Y' \\ Z' \end{pmatrix}, x = \frac{x'}{z'}, y = \frac{y'}{z'} \tag{2}$$

In first case for a three-dimensional space one cannot calculate coefficients based on came intrinsic and extrinsic parameters, whereas in second it is possible. Matrix  $R$  is and extended rotation matrix along the axes with shifts (3).

$$R = [R_\alpha \ R_\beta \ R_\gamma | t] \tag{3}$$

To reduce one dimension Z projection is replaced with a constant  $-h$ , that symbolizes a distance from camera to the ground (4).

$$\begin{pmatrix} r_{11} & r_{12} & r_{13} & t_x \\ r_{21} & r_{22} & r_{23} & t_y \\ r_{31} & r_{32} & r_{33} & t_z \end{pmatrix} \cdot \begin{pmatrix} X_w \\ Y_w \\ -h \\ 1 \end{pmatrix} = \begin{pmatrix} X_c \\ Y_c \\ Z_c \end{pmatrix} = \begin{pmatrix} a & b & c \\ d & e & f \\ g & h & i \end{pmatrix} \cdot \begin{pmatrix} X_w \\ Y_w \\ 1 \end{pmatrix} \tag{4}$$

If we write it in a system, we get (5).

$$\begin{cases} X_c = r_{11} \cdot X_w + r_{12} \cdot Y_w - r_{13} \cdot h + t_x = a \cdot X_w + b \cdot Y_w + c \\ Y_c = r_{21} \cdot X_w + r_{22} \cdot Y_w - r_{23} \cdot h + t_y = d \cdot X_w + e \cdot Y_w + f \\ Z_c = r_{31} \cdot X_w + r_{32} \cdot Y_w - r_{33} \cdot h + t_z = g \cdot X_w + h \cdot Y_w + i \end{cases} \tag{5}$$

From it can be attained that:

$$\begin{cases} a = r_{11} \\ b = r_{12} \\ c = -r_{13} \cdot h + t_x \\ d = r_{21} \\ e = r_{22} \\ f = -r_{23} \cdot h + t_y \\ g = r_{31} \\ h = r_{32} \\ i = -r_{33} \cdot h + t_z \end{cases}$$

This concludes, that with fixed projection  $Z = -h$  and  $3 \times 3$  matrix can be acquired from an extended matrix  $R$ . To get parameter values for the resulting matrix we make an assumption, that camera yaw angle is relatively small and can be neglected for the case of LDW. So rotation matrix consists only of pitch and roll. Since "birds-eye-view" suggests that camera is looking straight down, we provide additional 90-degree pitch rotation (6).

$$\begin{aligned} R_\beta \cdot R_\alpha \cdot R_{\alpha(90^\circ)} &= \begin{pmatrix} \cos \beta & -\sin \beta & 0 \\ \sin \beta & \cos \beta & 0 \\ 0 & 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \alpha & -\sin \alpha \\ 0 & \sin \alpha & \cos \alpha \end{pmatrix} \cdot \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \frac{\pi}{2} & -\sin \frac{\pi}{2} \\ 0 & \sin \frac{\pi}{2} & \cos \frac{\pi}{2} \end{pmatrix} = \\ &= \begin{pmatrix} \cos \beta & \sin \beta \cdot \sin \alpha & \sin \beta \cdot \cos \alpha \\ \sin \beta & -\cos \beta \cdot \sin \alpha & -\cos \beta \cdot \cos \alpha \\ 0 & \cos \alpha & -\sin \alpha \end{pmatrix} = \begin{pmatrix} r_{11} & r_{12} & r_{13} \\ r_{21} & r_{22} & r_{23} \\ r_{31} & r_{32} & r_{33} \end{pmatrix} \tag{6} \end{aligned}$$



Fig. 1. Original image from a calibrated camera.

By replacing  $r_{ij}$  with new values we get:

$$\begin{cases} a = r_{11} = \cos \beta \\ b = r_{12} = \sin \beta \cdot \sin \alpha \\ c = -r_{13} \cdot h + t_x = -\sin \beta \cdot \sin \alpha \cdot h + t_x \\ d = r_{21} = \sin \beta \\ e = r_{22} = -\cos \beta \cdot \sin \alpha \\ f = -r_{23} \cdot h + t_y = \cos \beta \cdot \cos \alpha \cdot h + t_y \\ g = r_{31} = 0 \\ h = r_{32} = \cos \alpha \\ i = -r_{33} \cdot h + t_z = \sin \alpha \cdot h + t_z \end{cases}$$

To acquire the resulting matrix one must multiply focal distance matrix with a transformation matrix (7).

$$\begin{pmatrix} f_x & 0 & c_x \\ 0 & f_y & c_y \\ 0 & 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} \cos \beta & \sin \beta \cdot \sin \alpha & -\sin \beta \cdot \sin \alpha \cdot h + t_x \\ \sin \beta & -\cos \beta \cdot \sin \alpha & \cos \beta \cdot \cos \alpha \cdot h + t_y \\ 0 & \cos \alpha & \sin \alpha \cdot h + t_z \end{pmatrix} = \begin{pmatrix} f_x \cdot \cos \beta & f_x \cdot \sin \beta \cdot \sin \alpha + c_x \cdot \cos \alpha & f_x(-\sin \beta \cdot \sin \alpha \cdot h + t_x) + c_x \cdot (\sin \alpha \cdot h + t_z) \\ f_y \cdot \sin \beta & f_y \cdot (-\cos \beta) \cdot \sin \alpha + c_y \cdot \cos \alpha & f_y(\cos \beta \cdot \cos \alpha \cdot h + t_y) + c_y \cdot (\sin \alpha \cdot h + t_z) \\ 0 & \cos \alpha & \sin \alpha \cdot h + t_z \end{pmatrix} \quad (7)$$

This is a resulting perspective transformation matrix acquired wholly from cameras extrinsic and intrinsic parameters, which can be applied in hardware solutions such as Still Image COProcessor (SIMCOP) on TDA platforms. The transformation was tested on a video from a calibrated camera (Fig. 1). With camera intrinsic and extrinsic parameters matrix was built and with help of OpenCV warp perspective function transformed video was constructed.

Camera parameter were:

$f_x = 1633.3333333333335$  focal length (in pixels);

$f_y = f_x$ ;

$c_x = 640$  - digital matrix horizontal center (in pixels);

$c_y = 480$  - digital matrix vertical center (in pixels);

$pitch = -2.026380478113274$  (degrees);

$yaw = 2.2671202323992437$  (degrees);

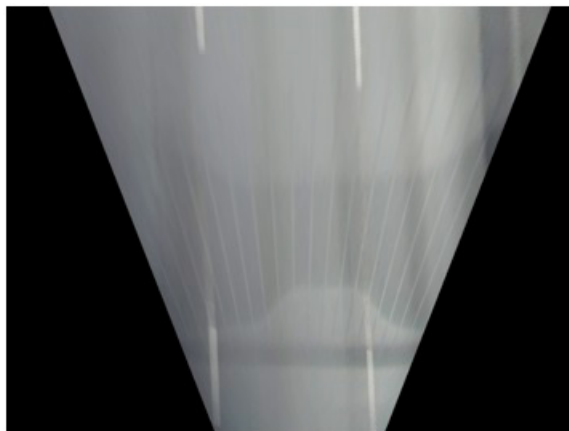


Fig. 2. Transformed imaged based on a  $3 \times 3$  matrix.

$roll = 0.5719324365448999$  (degrees);  
 $h = 1.1962422471370726$  (meters);  
 $t_x = 0.1595051172328819$  (meters, shift along  $X$  axis);  
 $t_y = 0$  (shift along  $Y$  axis);  
 $t_z = 0$  (shift along  $Z$  axis);

Resulting image provided expected results (Fig. 2).

## Conclusions

In this paper, we provided a formula for construction of a two-dimensional perspective transformation based on a three-dimensional but with a fixed  $Z$  projection. This method allows calculating transformation even on very small energy-efficient devices and furthermore the resulting matrix can be utilized with hardware solutions for perspective image transformations. Due to lack of extra surface projection step in a three-dimensional case the speed of an image construction increased by a multiple of two.

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